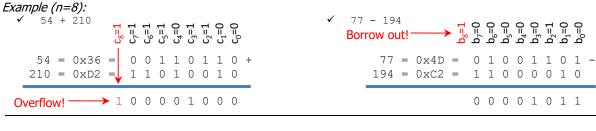
# **Homework 2**

(Due date: October 3rd @ 11:59 pm)

Presentation and clarity are very important! Show your procedure!

## **PROBLEM 1 (38 PTS)**

a) Perform the following additions and subtractions of the following unsigned integers. Use the fewest number of bits n to represent both operators. Indicate every carry (or borrow) from  $c_0$  to  $c_n$  (or  $b_0$  to  $b_n$ ). For the addition, determine whether there is an overflow. For the subtraction, determine whether we need to keep borrowing from a higher bit. (8 pts)



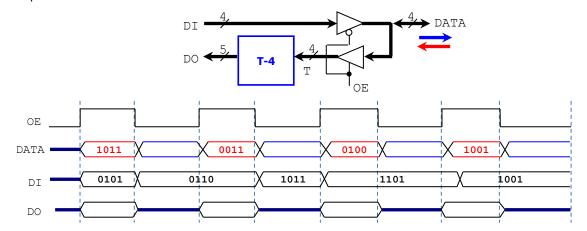
- $\checkmark$  23 + 403  $\checkmark$  77 128  $\checkmark$  103 + 204  $\checkmark$  199 107
- b) We need to perform the following operations, where numbers are represented in 2's complement: (24 pts)
  - $\checkmark$  -61 + 128  $\checkmark$  -126 + 263  $\checkmark$  225 + 31  $\checkmark$  -511 167  $\checkmark$  256 257  $\checkmark$  137 + 886
  - For each case:
    - ✓ Determine the minimum number of bits required to represent both summands. You might need to sign-extend one of the summands, since for proper summation, both summands must have the same number of bits.
    - Perform the binary addition in 2's complement arithmetic. The result must have the same number of bits as the summands.
    - ✓ Determine whether there is overflow by:
      - i. Using  $c_n$ ,  $c_{n-1}$  (carries).
      - ii. Performing the operation in the decimal system and checking whether the result is within the allowed range for n bits, where n is the minimum number of bits for the summands.
    - ✓ If we want to avoid overflow, what is the minimum number of bits required to represent both the summands and the result?
- c) Perform the multiplication of the following numbers that are represented in 2's complement arithmetic with 4 bits. (6 pts) 

  10101×0111, 0101×1001, 1100×1010

## PROBLEM 2 (7 PTS)

• Complete the timing diagram (signals *DO* and *DATA*) of the following circuit. The circuit in the blue box computes the signed operation T-4, with the result having 5 bits. T is a 4-bit signed (2C) number.

For example: if  $T=1010 \rightarrow DO = 1010 - 0100 = 11010 + 11100 = 10110$ .



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### **PROBLEM 3 (29 PTS)**

- In these problems, you MUST show your conversion procedure. No procedure ≡ zero points.
  - a) Convert the following decimal numbers to their 2's complement representations: binary and hexadecimal. (9 pts.) 
    √ -255.6875, 31.625, -128.6875

b) Complete the following table. The decimal numbers are unsigned: (6 pts.)

Decimal	BCD	Binary	Reflective Gray Code
127			
		10111010	
512			
			10010101
		11101010	
	100001110101		

c) Complete the following table. Use the fewest number of bits in each case: (14 pts.)

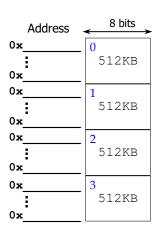
REPRESENTATION				
Decimal	Sign-and-magnitude	1's complement	2's complement	
-120				
			10101000	
		0111010001		
			1000000	
	1001111			
-64				
			10000011	

## **PROBLEM 4 (26 PTS)**

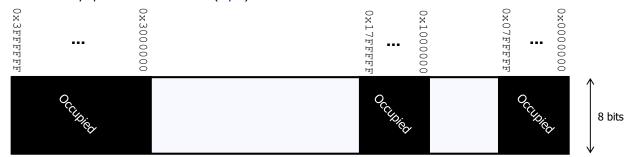
- a) What is the minimum number of bits required to represent: (2 pts)
  - ✓ 32678 memory addresses in a computer? ✓ Numbers between 0 and 2048?
- b) A microprocessor has a 32-bit address line. The size of the memory contents of each address is 8 bits. The memory space is defined as the collection of memory positions the processor can address. (6 pts)

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- What is the address range (lowest to highest, in hexadecimal) of the memory space for this microprocessor? What is the size (in bytes, KB, or MB) of the memory space? 1KB =  $2^{10}$  bytes, 1MB =  $2^{20}$  bytes, 1GB =  $2^{30}$  bytes
- A memory device is connected to the microprocessor. Based on the size of the memory, the microprocessor has assigned the addresses  $0 \times 40800000$  to  $0 \times 40BFFFFF$  to this memory device.
  - What is the size (in bytes, KB, or MB) of this memory device?
  - What is the minimum number of bits required to represent the addresses only for this memory device?
- Address
  0x40800000
  0x40800001
  ...
  0x40BFFFFF
- c) A microprocessor has a memory space of 2 MB. The size of the memory contents of each address is 8 bits (1 byte). (7 pts)
  - ✓ What is the address bus size (number of bits of the address) of this microprocessor?
  - ✓ What is the range (lowest to highest, in hexadecimal) of the memory space for this
    microprocessor?
  - ✓ The figure (right) shows four memory chips that are placed in the given positions:
    - Complete the address ranges (lowest to highest, in hexadecimal) for each of the memory chips. (5 pts)



- d) The figure below depicts the entire memory space of a microprocessor. Each memory address occupies one byte. (11 pts)
  - What is the size (in bytes, KB, or MB) of the memory space? What is the address bus size of the microprocessor?
  - If we have a memory chip of 8MB, how many bits do we require to address 8MB of memory? (1 pt.)
  - We want to connect the 8MB memory chip to the microprocessor. For optimal implementation, we must place those 8MB in an address range where every single address share some MSBs (e.g.: 0x0000000 to 0x07FFFFF). Provide a list of all the possible address ranges that the 8MB memory chip can occupy. You can only use any of the non-occupied portions of the memory space as shown below. (8 pts)



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